


BIOMATH
 Department Applied Mathematics,
 Biometrics and Process Control

The Usefulness of Models in Environmental Engineering

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Models in Control...



De nieuwe Citroën Xsara.
Getest en goedgekeurd door
Claudia Schiffer.

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Overview

- **Models**
 - What are they?
 - How do I build them ?
- **Application of Models**
 - Understanding / Education / Training
 - Experimental Design
 - Intelligent Sensors
 - Model-based Control
 - Decision support (Risk Assessment - System Design)

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Definitions

- **System**
Part of reality that is separated from its environment on the basis of a purpose defined by the researcher
- **Model**
An approximate description of a part of reality considering only those aspects of interest
- **Simulation**
= Virtual Experimentation: Manipulation of a model to gain insight in the "behaviour" of the real system

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Types of Models

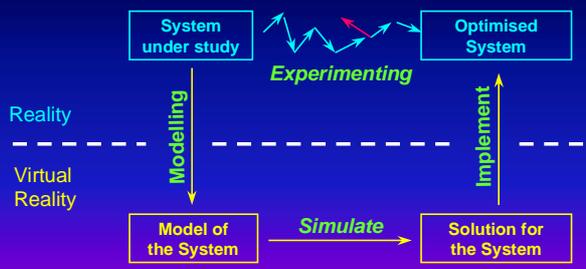
- **Mental models** (ideas, concepts, ...)
- **Verbal models** ("description in words")
- **Scale models** ("house in cardboard")
- **Computer models** ("house in AutoCad")
- **Mathematical models** ("equations")

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Why Modelling ?

Solving Problems for complex systems



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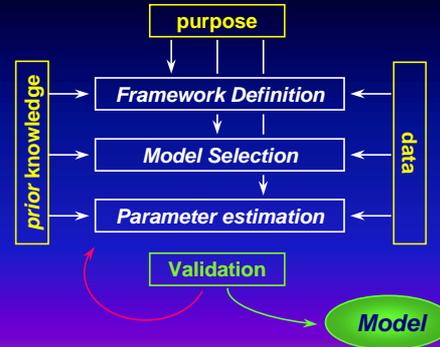
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Model building: Starting points

- **Purpose of the model**
 - Increasing understanding of a system *(Think tank)*
 - Summary of knowledge/data *(Communication)*
 - Prediction of future behaviour *(Control)*
- **Prior knowledge**
 - Experience
 - Existing models
 - Literature (facts, phenomena, theories, ...)
- **Data**
 - Existing data
 - New data collected in view of model building

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Model building: Subtasks



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Models to the General Public

$$E = mc^2$$

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Models to the General Public



Weather Forecasting



(Reading, UK)

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Models in Environmental Engineering

Only two types of application:

- **Describing the past ($E=mc^2$)**
 - Understanding (research - education - training)
 - Summary of knowledge
- **Prediction of the future (*Weather*)**
 - Forecasting the future state of an existing system
 - Forecasting the future behaviour of a changed system

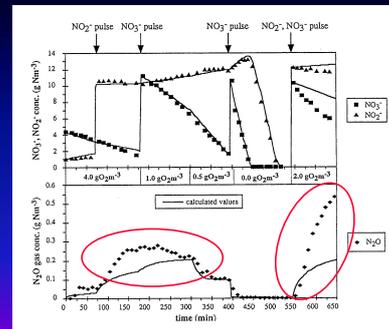
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Models for understanding

- Hypothesis is generated on the basis of
 - data as such (apple falls off a tree -> model)
 - discrepancy of data with an existing model
- New insight is acquired when the new model is accepted by the scientific community
 - ... until the next (better) data set comes along...

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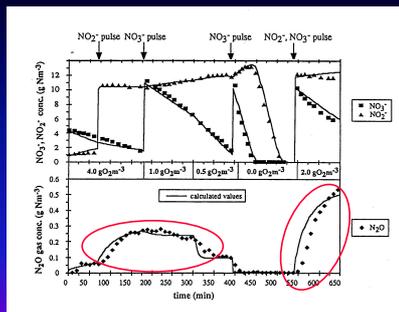
Understanding N₂O emissions



Model is insufficiently "flexible"

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Understanding N₂O emissions

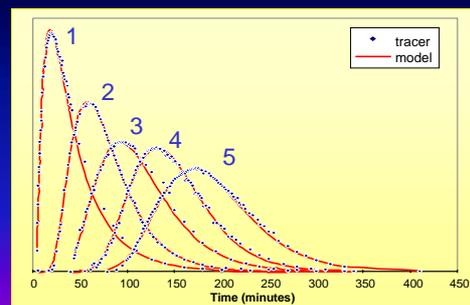


Model is much better !

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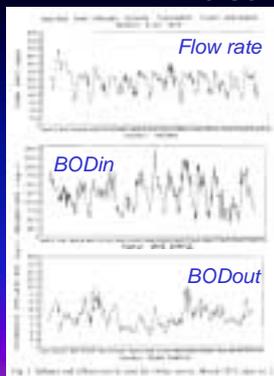
Models for description/summary

Mixing behaviour in a river (only 5 numbers !)



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Time series of data



Summary of data:

Time series models:

$$\begin{aligned} \text{Bout}(t) = & 0.55 \text{ Bout}(t-1) + 0.3 \text{ Bout}(t-7) \\ & + 0.49 \text{ Bin}(t) - 0.12 \text{ Bin}(t-1) \\ & - 25 \text{ dt}(t) + 32.5 \text{ dt}(t-1) - 6.7 \text{ dt}(t-7) \\ & - 0.3 \text{ SSin}(t-1) + 0.22 \text{ SS}(t-2) \\ & + N(t) \end{aligned}$$

The whole data series is condensed into a few numbers (only 9)!

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Use of models for Optimal Experimental Design (OED)

- Purpose of experimental design: create experimental conditions such that data allow
 - model selection
 - accurate parameter estimation
 - validation of a model

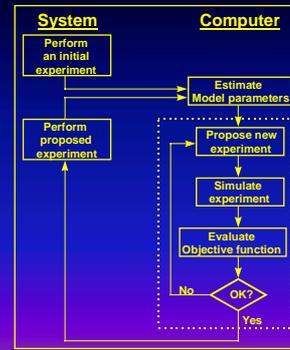
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Questions to be answered by Experimental Design

- What variables should we measure ?
- What is the required accuracy ?
- Over what period should be measured ?
- At what frequency are the data to be collected ?
- At what location should the measurements be done ?

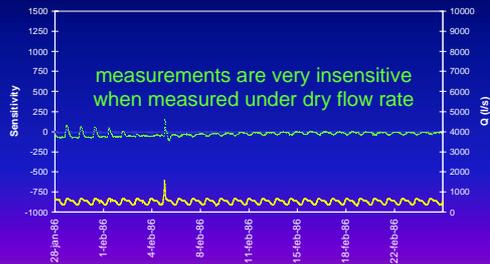
Quantified in an Objective Function to be optimised by the OED algorithm

Model based Experimental Design



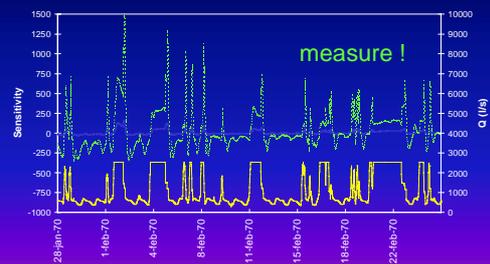
Application of OED

Calculated sensitivity to a settling parameter during dry weather conditions



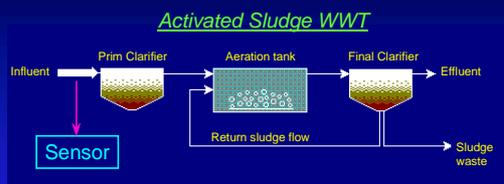
Application of OED

Calculated sensitivity to a settling parameter during wet weather conditions



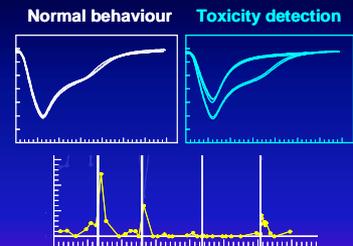
Intelligent sensors

- Raw data + Model



Intelligent sensors

2 series of 5 respirograms in 2h



No action leads to pollution

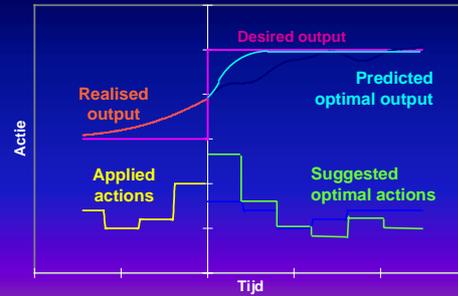
Control prevents pollution

Use of Models in Process Control

- **Controllers with built-in model**
eg. Model based predictive control
- **Support during the design of the control structure**
Choice of actuators, sensors, control laws
- **Support during the tuning of controllers**
eg. Tuning the parameters of a PID-controller
- **Prediction of disturbances**
eg. Rain - runoff / diurnal waste flow pattern

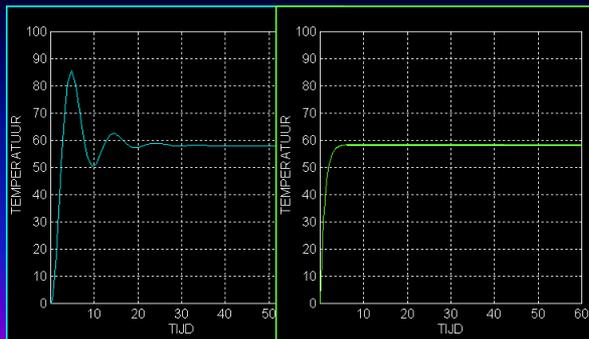
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Model-based Control: MBPC (Model Based Predictive Control)



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Controller tuning



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Use of Models in Decision Support

- Wastewater treatment plant design using Economic Cost calculations ==> MoSS-CC
- Integrated urban water management using sewer/WWT/river models ==> Brussels
- Environmental Risk Assessment of "down-the-drain" chemicals ==> GREAT-ER

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MoSS-CC project

Model based Simulation System for Cost Calculation

- Calculation of the investment cost of a new or upgrade WWTP design
- Calculation of the (fixed & variable) operating costs of a new or upgrade WWTP design

=> Better design

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Investment Cost Relationships

- Power laws are applied:

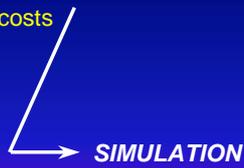
$$COST = \Theta(\text{Process Size})^n$$

- **Process size:** an easy to measure plant characteristic:
 - volume
 - area
 - length
 - design flow rate
 - pumping capacity
 - installed mechanical power

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Operating Cost Relationships

- Maintenance costs ==> proportional to investment
- Sludge treatment/disposal costs
- Pumping energy
- Aeration energy
- Mixing energy
- Effluent taxes



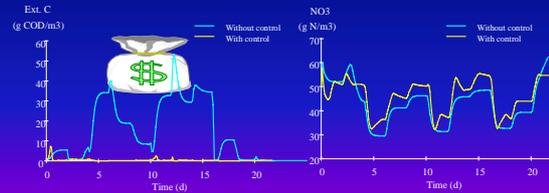
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Example of Cost Reduction

- Industrial plant with nitrogen problem:
Question: Include automatic control or not?

External Carbon for Denitrif.

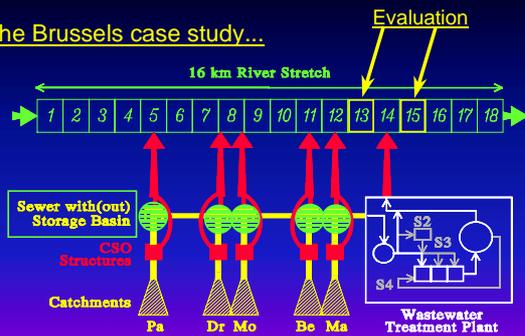
Effluent nitrate conc.



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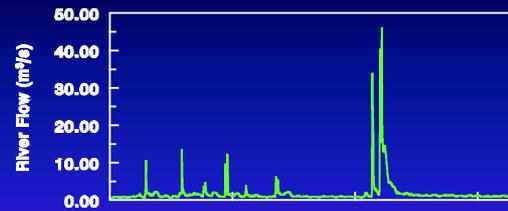
Integrated Urban Water Management

The Brussels case study...



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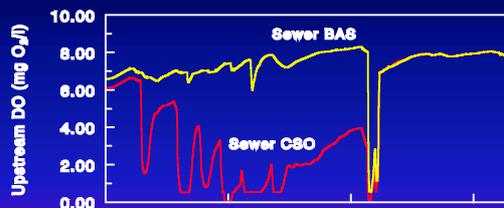
Effect of 2 design options (BAS/CSO) on River Water Quality



One big and several small rain events in summer '86

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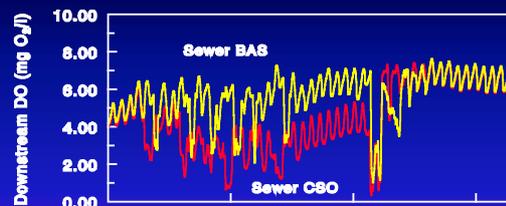
River Water Quality (oxygen) Downstream of CSO, Upstream of WWTP



Clear beneficial effect of retention basins (BAS) in sewer!

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River Water Quality (oxygen) Downstream of CSO, Downstream of WWTP



Beneficial effect of basins is reduced due to lower efficiency of WWTP by increased loading from basins

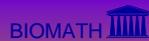
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GREAT-ER project

Geography-referenced Regional Exposure Assessment Tool for European Rivers

- prediction of the fate of specific "down-the-drain" chemicals in surface water
- using Geographical Information Systems (GIS)
- for use within Environmental Risk Assessment

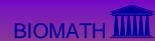
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Environmental Risk Assessment

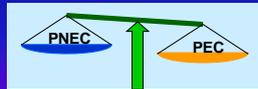
- Aim = **assess** the probability and severeness of negative **effects** on ecosystems after exposure to **chemicals**
- steps:
 - **exposure:** Predicted Environmental Concentration (**PEC**)
→ how much ends up in the environment ? where ?
 - **effects:** Predicted No Effects Concentration (**PNEC**)
→ how toxic / dangerous is the chemical for the environment ?

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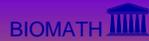


Environmental Risk Assessment

- Aim = **assess** the probability and severeness of negative **effects** on ecosystems after exposure to **chemicals**
- steps:
 - **exposure:** Predicted Environmental Concentration (**PEC**)
 - **effects:** Predicted No Effects Concentration (**PNEC**)
 - **risk ratio:** $\frac{PEC}{PNEC} < 1 ?$

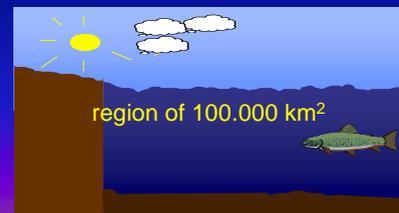


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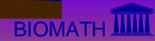


Environmental exposure assessment

- **Current methods** (advised in EU legislation):
 - **multimedia fate models**



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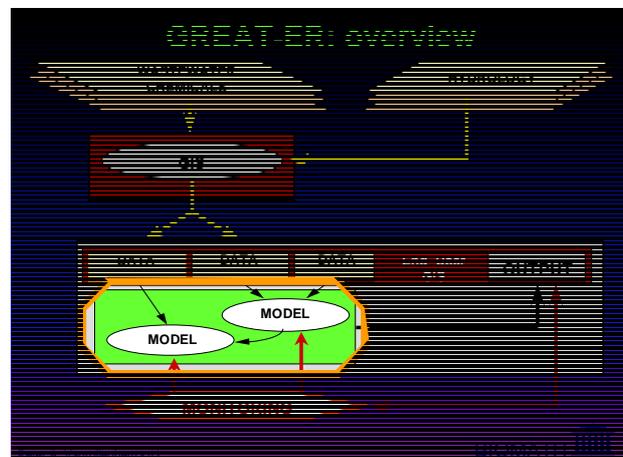
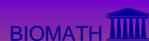


Environmental exposure assessment

- **Current methods:**
 - **multimedia fate models**
 - no spatial nor temporal variability considered
→ limited accuracy **FACTOR > 100-1000 !**
- **GREAT-ER: refine PEC calculations**
 - 'real' geo-referenced data
 - variability
 - geo-referenced → **validation** is possible

AIM = **FACTOR < 3-5**

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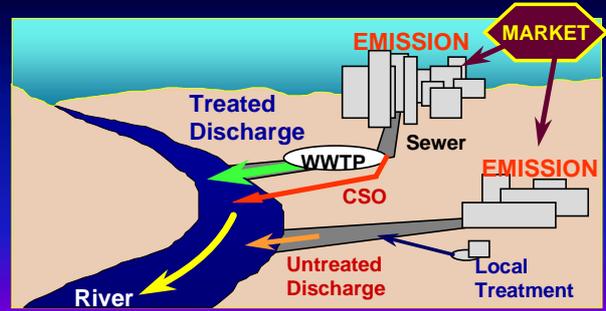
Overall simulation approach



- 'Steady state' models (no dynamics)
- Stochastic / deterministic
- Input / Output - Statistical distributions
- Geo-referenced

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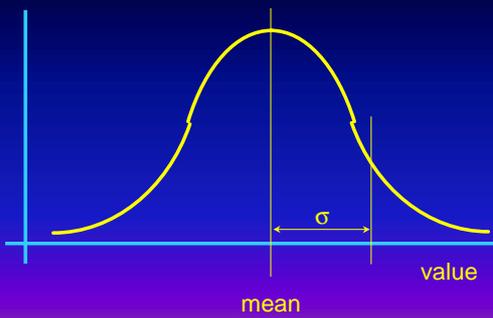
Deterministic Model



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Stochastic simulation

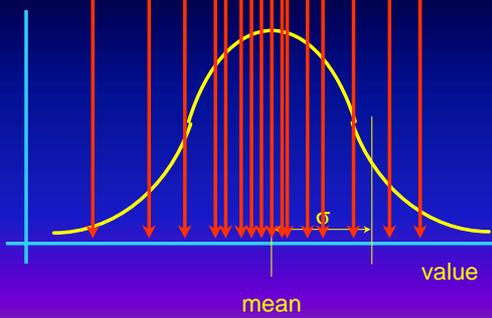
frequency for every variable/parameter



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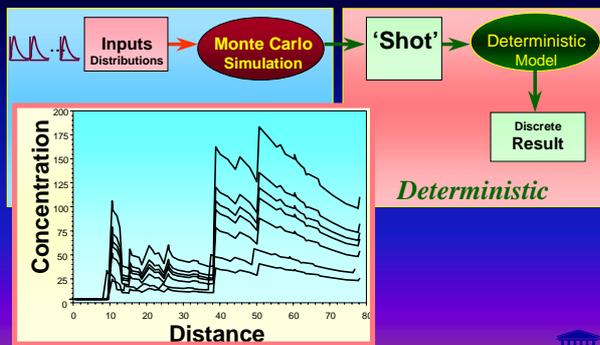
Monte Carlo simulation

frequency Shots



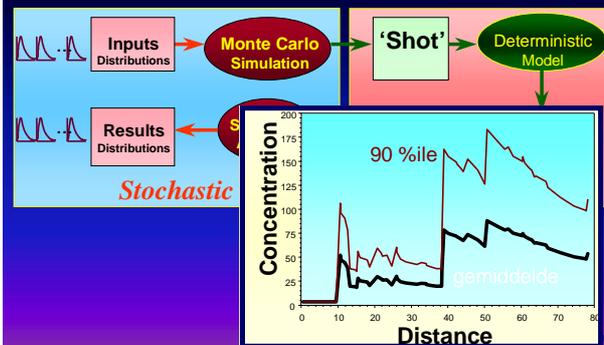
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Stochastic simulation



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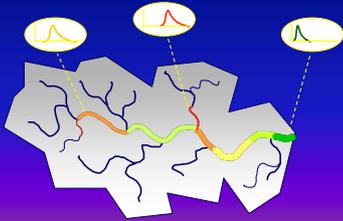
Stochastic simulation



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Analysis

- direct GREAT-ER simulation results
geo-referenced predicted concentrations



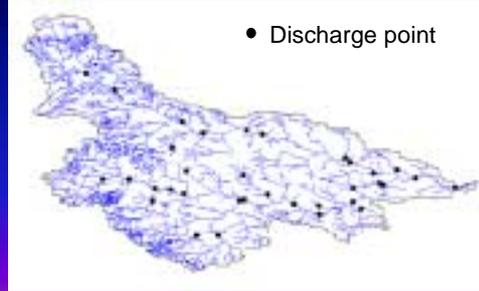
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GREAT-ER Validation

Catchment in Yorkshire (UK)

- Discharge point

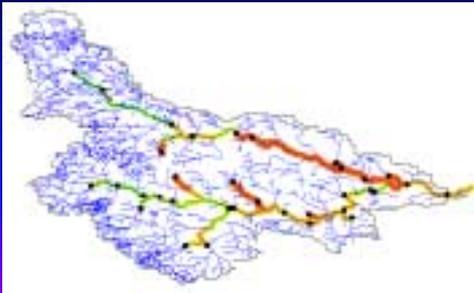


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GREAT-ER Validation

LAS concentrations in the river stretches

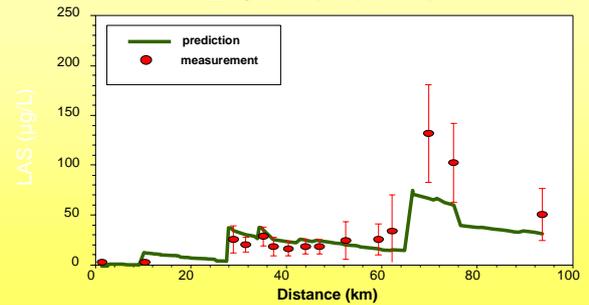


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Validation of GREAT-ER

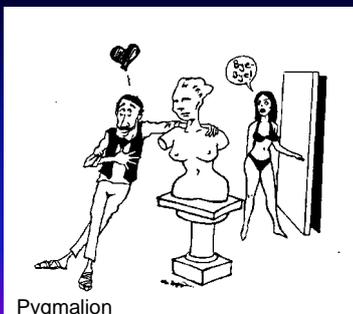
LAS in the main river



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“Do not fall in love with your model”



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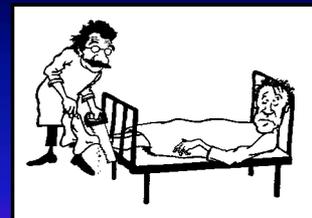
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Epilogue

Models are and can be very useful,
but they are only an approximate description of reality

Procrustes bed:
(Greek mythology)

“Do not adjust reality
to the model!”



Modelling should be done
with knowledge in the field !

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